

Autopoiesis, Cognition, and Evolution

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Question: What conceptual primitives best found a study of distributed cognition?

Outline

1 Introduction

- A word of thanks
- Scientific question

2 Compression and elaboration

3 Mathematical foundations

4 Conclusion

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Doug, I hope that the results of this work help to recharge your own energy stores at AFOSR, i.e. that my work is useful to those who make it possible. 1

Conceptual primitives

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- *Conceptual primitives*: basic concepts and their rules of composition.

I don't claim to know the answers, so let's think together.

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1 Introduction

2 **Compression and elaboration**

- Some conceptual primitives
- Distributed cognition
- What it's all for?

3 Mathematical foundations

4 Conclusion

Some conceptual primitives

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 - DNA compresses the lessons of past lives.
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 - Scientific theories compress natural phenomena in language.
 - Theories are elaborated in laboratories to channel phenomena.
- Prediction and betting: *we are predictions / bets*
 - Your knees are a prediction that gravity will be in some range.
 - Your lungs are a prediction that air pressure will be in some range.
 - Past *lessons*—bets won and lost—encoded as current structure.

Cognition

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- My mind, like DNA, compresses the lessons of my past.
- Present cognition, like living, elaborates the compressed stuff.
- All of this serves as an experiment on the present situation.

Distributed cognition

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- I use my computer, or just pencil and paper: offloading cognition.
- I use interactions with you, scientific articles and videos.
- My brain is not one atomic unit; it is already distributed cognition.

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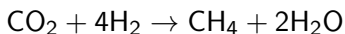
Existing systems are integrated to pursue a common goal.

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One answer: dissipating energy; channeling potential differences.

- Earliest life channeled high-energy emissions from geothermal vents

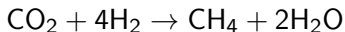


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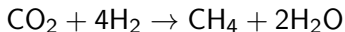
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Complex cognition is required to dissipate energy at scale.

- Team members distribute cognitive load.
 - Scientists, engineers, financial backers, drill operators, etc.
 - Each acts—releases stored energy—in order to make it happen.
 - Communication is required to translate problems and solutions.
- If the total effort is successful, team members are recharged, repaid.

A mathematical ground for autopoiesis?

Autopoiesis means self-production.

- An ant colony, a cell, a football team, capitalism, one's mind.
- These systems repeatedly channel energy through themselves.
- They expend energy now, and are recharged later.
- They adapt to changing environments.
- They act to successfully predict futures in which they exist/flourish.

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- What is it?
- How are autopoietic systems assembled?
- How to conceptualize their evolution / adaptation/ structural drift?
- How and when do they join into larger assemblies?

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What mathematical primitives best found this study?

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1 Introduction

2 Compression and elaboration

3 **Mathematical foundations**

- Applied category theory
- Example formalism: wiring diagram operads
- Memoryless dynamical systems generate
- Dynamic rewiring

4 Conclusion

Category theory

Category theory is the most efficient known thought-compression language.

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Category theory is mathematics, form-fit to any technical subject.

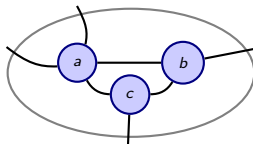
- Consists of conceptual primitives and principles for combining them.
- Data, software, business processes can all be compressed into CT.

Example: wiring diagrams

Wiring diagrams can be interpreted according to a variety of semantics.

- E.g. tensor networks, relational algebra, dynamical systems.
- Each is called an *algebra*; construct new terms from old.

Wiring diagrams can be nested.

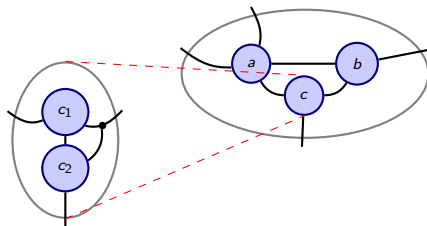


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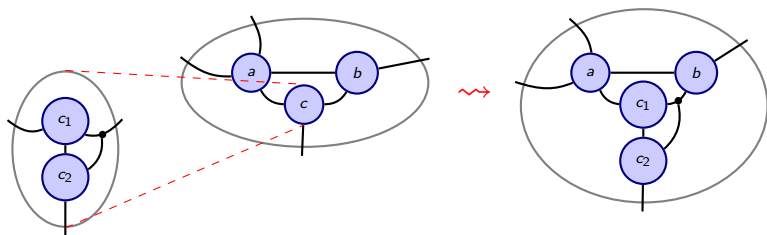


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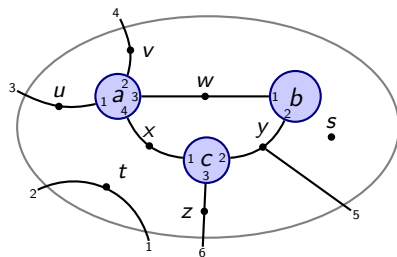
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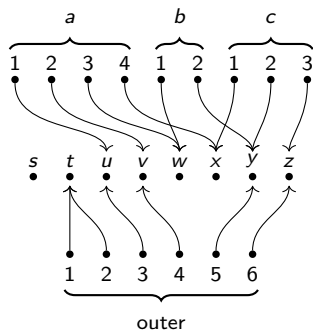
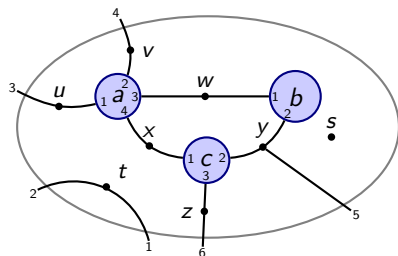
Mathematics of wiring diagrams

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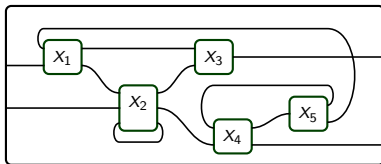
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Wiring diagrams are encoded mathematically via sets and functions.

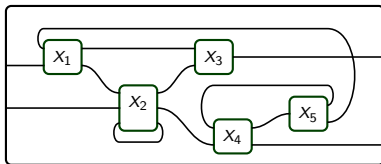
Memoryless tests generate all dynamical systems



Open discrete dynamical system (DDS) = stream processor

- Input streams drive the system through state space.
- The system outputs a stream which is passed to another system.
- Wiring all these together you get a more complex system.

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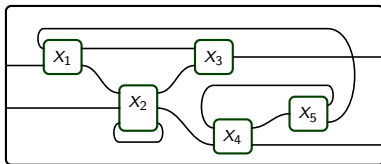
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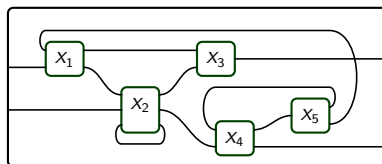
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- Upshot: simplist systems, wired together, become arbitrarily complex.

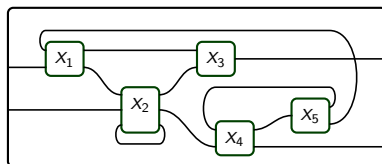
Mode-dependent networks of dynamical systems



In algebra of DDSs, each cell is inhabited by a dynamical system

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We can also allow the interface to change shape based on system *modes*.

- Each cell's state determines its “communicative mode.”
- This mode determines the input/output shape of the cell's interface.
- The modes of everyone in the network jointly determine the wiring.
- Idea: I can close or open my eyes; we can decide to connect.

Mode-dependent networks in autopoiesis?

Goal: a compositional framework for studying autopoiesis.

- The above is about systems that dynamically change wiring pattern.
- But there's no "why", no goals, no sense of direction.
- Can we somehow encode:
 - Energy dissipation?
 - Selectivity, adaptation, evolution, cognition, autopoiesis?

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I imagine that systems want predictable environments rich in free energy.

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This is the current status, one way we might look at autopoiesis.

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- ...if it'd lead us to more free energy, more low-hanging fruit.
- What are the conditions by which such a team forms and persists?

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